A topic-focused trust model for Twitter

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A B S T R A C T

Twitter is a crucial platform to get access to breaking news and timely information. However, due to questionable provenance, uncontrollable broadcasting, and unstructured languages in tweets, Twitter is hardly a trustworthy source of breaking news. In this paper, we propose a novel topic-focused trust model to assess trustworthiness of users and tweets in Twitter. Unlike traditional graph-based trust ranking approaches in the literature, our method is scalable and can consider heterogeneous contextual properties to rate topic-focused tweets and users. We demonstrate the effectiveness of our topic-focused trustworthiness estimation method with extensive experiments using real Twitter data in Latin America.

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1. Introduction

As one of the most popular social messaging tools, Twitter is experiencing a tremendous growth. The number of users is over 200 million as of 2013, contributing over 200 million of tweets every day [1]. The posts in Twitter can be about any domain and any topic in the world, ranging from daily conversations to socially crucial issues. Thanks to the 140 character limitation of length, “timeliness” and “brevity” become the most distinguishing features of tweets. This empowers the freshness of the Twitter posts which usually beat traditional breaking news broadcasting media. Therefore, Twitter is becoming a promising information source to get the most timely knowledge and news around us [2]. Since different users may favor information of different topics, how to identify credible tweets belonging to the specific topics according to users’ interests is of great importance. This paper is particularly concerned with the issue of how to treat Twitter as a news channel and use our proposed trust model to identify trustworthy tweets/users.

Despite the advantages of timeliness, Twitter suffers from the fact that it is hardly a trustworthy news resource. First, tweets are usually posted by individual users instead of news authorities. The trustworthiness of tweets or users is hard to be ascertained. Second, the spread of tweets in Twitter is through social networks instead of formal news broadcasting like traditional media. In Twitter, the trustworthiness of tweets/users can only be estimated through indirect means, such as the number of followers of a user or a tweet, and the number of retweets of a tweet. This is potentially problematic and can even foster the spread of rumors, because a malicious user can easily forge followers or retweets. Finally, the noisy nature of tweets (largely due to unstructured languages and abbreviations) further hinders accuracy of trustworthiness assessment. Tweets are often written in a casual style, without following standard grammatical rules. For example, there is no verb in the tweet “Pretty bad day ioi waiting for it to go by already”. New abbreviations and slangs are emerging each day, such as TMB (tweet me back) and abt (about). These noises make it difficult to understand tweets and to properly assess their trustworthiness.

Considering the social impact of information trustworthiness in Twitter, currently there is significant interest on trustworthiness evaluation of tweets or users [3,4]. A thread of works focused on the evaluation of credibility of tweets by inspecting the contextual contents of tweets [5–10]. Typically, key features indicating the quality/credibility, such as the length and the language style, are chosen as the features to train a classifier using tweets manually labeled as credible and incredible. Another thread of works focused on investigating the trustworthiness of the users by considering the underlying social network structure of Twitter through the numbers of followers and retweets and the social relationships between users [11–14].

We observe a number of deficiencies in the works cited above and aim to devise an effective trustworthiness estimation method to remove these deficiencies:

1. Most of current work focused on evaluating the credibility of general tweets. Credibility evaluation for topic-focused tweets of users’ interest is of significantly practical use, yet has not been well studied. Supervised learning method is often applied
to identify the tweets of specific domains; however, it is not scalable to manually label credible and incredible tweets for supervised learning. To build a training dataset for supervised learning, current technologies require extensive human effort to label tweets. Moreover, labeling of tweets in the training dataset must be updated periodically. There is a need to automatically rate tweets dynamically for scalability. In our work, we do not use supervised learning so there is no need building a training set.

1. Untreated in the literature, we assess trustworthiness of users/tweets by a novel topic-focused trustworthiness estimation method. We propose a new design notion of similarity-based trust evaluation by which a candidate tweet is considered trustworthy if it is non-conflictingly similar in contextual properties against trustworthy tweets or trustworthy news reports from broadcasting stations. Twitter data are noisy and pointless. However, we can “infer” trust from trustworthy news reports to noisy tweets if there is a sufficient context similarity between news reports and tweets, considering textual, spatial, and temporal contextual properties. Our method is scalable and can consider heterogeneous contextual properties to rate topic-focused tweets/users.

2. Prior works consider the social and contextual relationships between users/tweets for trustworthiness estimation dynamically by means of a novel iterative trust propagation algorithm.

3. Prior works are based on a social graph trust model [4] with which the credibility of a user is determined by its surrounding neighbors, e.g., how many social connections a user has. However, the social graph model is often constructed without considering the possibility that the edges in the graph can be artificially manufactured by a malicious user. One example is political astroturf, where political campaigns fake as spontaneous “grassroots” that are actually carried out by a malicious plotter or a conspiracy organization [15]. Our work is also based on social graphs. However, we do not use the social graph for directly inferring tweet trustworthiness. Rather, we rate topic-focused tweets by means of a novel similarity-based trust evaluation mechanism and then use the social and contextual relationships described by a social graph for trust propagation dynamically to achieve trust accuracy.

4. Prior works consider that trust is context independent, i.e., trust is deterministic in any situation and any context. However, in reality, trust is context dependent. A node may be trustworthy in one context, but not in another context. For example, a doctor is not as trustworthy when talking about laws, compared with medicine. In our work, we consider textual, spatial and temporal contextual features as we estimate trustworthiness of one user/tweet against another user/tweet.

In this paper, we propose a novel method to estimate the user/data trustworthiness in Twitter. Our method first accurately identifies topic-focused trustworthy tweets, and then updates the user/data trustworthiness through iterative trust propagation. To address the scalability issue, we apply our similarity-based trust evaluation method with contextual heterogeneous properties to rate users/tweets against trustworthy users/tweets (say from authorities) without the need of human efforts in labeling credible tweets for supervised learning. As shown in Fig. 1, our system consists of two main components: topic-focused similarity-based trust evaluation and trust propagation. The first module rates users/tweets against trustworthy users/tweets for the initial trustworthiness scores, and then the second module further propagates trustworthiness scores among tweets. Our contributions are as follows:

1. We propose a novel trust propagationalgorithm which iteratively re-estimates the trustworthiness of users/tweets, by jointly considering their social and contextual relationships in a Twitter social graph. The theoretical proof of convergence is demonstrated.

2. We demonstrate the scalability of our topic-focused trustworthiness estimation method with raw tweet data (Latin America civil unrest tweets) without the need to manually label credible and incredible tweets in a training set for supervised learning.

2. Related work

In this section we survey the state of the art in user and tweet trustworthiness estimation in Twitter. Existing approaches in general can be categorized into two types, namely, feature-based trust ranking [5–9,11,12,16–18,35–37], and social graph based trust ranking [10,13–15,19–22,38,39]. We discuss them in Sections 2.1 and 2.2, respectively. In particular, we survey the subject area of tweet trustworthiness in [5–10,16]; user trustworthiness in [11–14,35–37]; rumor and misinformation propagation in [15,21,22,38,39]; supervised learning based on classification in [5,6,8,35,37]; and unsupervised learning based on clustering in [17–20].

2.1. Feature-based trust ranking

Existing works in this category in general classify tweets related to a target topic based on credibility “features” of tweets and then apply supervised learning to classify if a tweet is credible. Gupta et al. [8] provided a SVM-rank based system TweetCred to assign a credibility score to tweets in a user’s timeline. Ravikumar et al. [11] studied features that affected user perception. Shariff et al. [16] identified eight features that cannot be automatically identified from tweets, but are perceived by users as important when judging information credibility. Weerkamp and de Rijke [6] used several credibility indicators and divided them into post-level (e.g., spelling, timeliness and document length) and blog-level (e.g., regularity, expertise, and comments). Based on these credibility indicators, they proposed a series
of credibility ranking methods to find top credible tweets. They concluded that using the post-level indicators combined with comments and pronouns can provide the best performance. Morris et al. [9] conducted controlled experiments to study the impact of several tweet features (message topic, user name, and user image) on the user perception of tweet truthfulness. They showed that user judgments on tweet truthfulness are biased, and often are based on heuristics (e.g., retweeting). Yang et al. [12] studied the impacts of several microblog features such as gender, name style, profile image, location, degree of network overlap with the reader, on the credibility perception of users from different countries. They demonstrated that cultural differences can result in different perceptions on user credibility. For example, Chinese users are easier to trust pseudonymously authored tweets and have a strong dependence on microblogs as an information source. Duan et al. [7] studied three types of features: content relevance features (i.e., length and similarity), Twitter specific features (i.e., whether a tweet contains a URL link), and account authority features (i.e., the number of followers). They concluded that URL and time information contained in a tweet are the most effective features for tweet credibility. Todd et al. [35] evaluated user trustworthiness through a classifier trained by multiple features, such as the number of followers, friends, and tweet posts. Tweet posts by credible users are retained for analysis, while those written by untrustworthy users are discarded. Yeau et al. [36] modeled user trust using the Analytic Hierarchy Process for measuring trust in a multi-criteria scenario (e.g., followers, retweets, and mentions). Their approach could integrate perception and sentiment of analysts into the problem solving process. Castillo et al. [5] applied a supervised learning classification model to classify tweets as credible or not based on features extracted including message, user, topic, and propagation based features. Li et al. [37] proposed an approach to train a classifier that, starting with some labeled data, identifies trustworthy users through profile/content/graph/neighbor features, propagates trust through the social network, and finally reuses the most trustworthy users to retrain the classifier. Given a set of human participants of unknown trustworthiness together with their sensory measurements, [17,18] applied Bayesian reasoning and maximum likelihood estimates to determine the probability that a given measurement is true. Relative to the works cited above, our topic-focused trustworthiness estimation method is efficient and scalable, as it does not need to label credible and incredible tweets in a training set for supervised learning.

2.2. Graph-based trust ranking

In contrast to feature-based trust ranking, graph based trust ranking infers trustworthiness information through social connections by means of a social graph. Ravikumar et al. [10] proposed RAPProp which combines two measures of trustworthiness of a tweet. One measure is the trustworthiness of the source of the tweet, which may be a user, a retweet or a webpage cited in the tweet. Another measure estimates tweet trustworthiness by analyzing the tweet content to discover the tweet’s corroborating relationship with other tweets. Magdalini and Iraklis [38] evaluated trust and distrust of users by implicit or explicit recommendations received from other users through user-to-user social connections. Based on social similarity between neighboring nodes, [39] explored the local structure of social networking by means of a graph pruning technique, and evaluated combined trust and distrust through a variation of Page–Rank Algorithm. Abbasi and Liu [13] measured the credibility of social media users based on their online behavior. Users with similar behavior are clustered together and are assigned similar credibilities. However, they failed to give a clear picture about user behavior. To rank credibility of tweets on a topic, [14] proposed to build a social graph modeling web documents, tweets, and users. By connecting users who share similar contents, the social graph is capable of linking tweets and web documents, filtering informal writing and noise, and inferring unseen relationships between users and tweets from explicit ones. Kang et al. [19] considered tweet trustworthiness as “believability that can be assigned to a tweet about a target topic” and provided three strategies for credibility computation: user-level, content-level, and hybrid. User-level strategies make use of dynamics of information flow from the underlying social network to compute credibility ratings for users. Content-level strategies identify topic patterns and tweet properties which can lead to positive feedback such as re-tweeting and/or credible user ratings. Hybrid strategies combine user-level and content-level strategies by using a weight, cascade or filter connector. Relative to the works cited above, our approach is also based on social graphs. However, we do not use the social graph for inferring tweet trustworthiness. Rather, we rate topic-focused tweets by means of a novel similarity-based trust evaluation mechanism and then use the social and contextual relationships described by a social graph for trust propagation dynamically to achieve trust accuracy. Zhao et al. [20] ranked tweets through relevance to the query, aiming to identify latent spatial events based on the tweet graph built. Our work is different from [20] in that we intend to evaluate tweet credibility. [15,21,22] studied rumor propagation in social networks. Jin et al. [21] identified rumors relevant to Ebola outbreaks using dynamic query expansion. Rakieiwicz et al. [15] studied astroturf political campaigns on microblogging platforms by using multiple centrally-controlled accounts to create the appearance of widespread support for a candidate or opinion. Kwon et al. [22] proposed to identify rumors by examining the following three aspects of diffusion: temporal, structural, and linguistic. Different from the above cited works, our approach is to assign trustworthiness scores to tweets to differentiate trustworthy tweets from rumors.

3. Problem formulation

In this section, we begin with a few key concepts, and then we formally define the problem we are solving and the two major tasks in our protocol design for solving the problem.

Definition 1. Twitter collection: a Twitter collection denoted by \( C = \{C_1, C_2, \ldots, C_T\} \) is a collection of time-ordered Twitter data separated by \( T \) time intervals, where \( C_t \in C \) represents the subcollection of the \( t \)-th time interval. A Twitter subcollection \( C_t \) is captured by a Twitter social graph which we call a Twitter heterogeneous information network in this paper.

Definition 2. Twitter heterogeneous information network: a Twitter heterogeneous information network (for describing a Twitter subcollection) is an undirected graph \( G = (V, E) \). \( V = W \cup D \cup U \) where \( W \), \( D \) and \( U \) denote the node sets of “words,” “data” (i.e., tweets) and “users,” respectively. \( E \subseteq V \times V \) stands for the undirected edge set.

Fig. 2 illustrates an instance of the Twitter heterogeneous information network. The \( t \)-th word is denoted as \( W_t \). Similarly, \( D_t \) and \( U_t \) stands for the \( j \)-th tweet and the \( k \)-th user. A tweet can contain geo-information location denoted as \((R_t)\), and timestamp information denoted as \( t(D_t) \). The edge set \( E \) consists of the relationships among heterogeneous entities, such as “replying” between “tweets,” “authorship” between a “user” and a “tweet,” and “containment” between a “term” and a “tweet.”

Definition 3. Trustworthiness score: the trustworthiness score denotes the degree that a tweet or a user is deemed credible. We will simply use “trustworthiness” to refer to “trustworthiness score” for short when the context is clear. Mathematically, we denote the trustworthiness of a tweet \( D_t \) as \( R(D_t) \) while we denote the trustworthiness of a user \( U_j \) by \( R(U_j) \).

The trustworthiness of a tweet can be estimated by whether its content refers to things that really happened. The trustworthiness of a user can be estimated by the user’s posts. Trustworthiness is
context-dependent. In other words, it depends on specific topic domains, e.g., sports, laws, civil unrest. For example, a user who is a doctor is not as trustworthy when talking about laws as when this user is talking about medicine.

Definition 4. Event: an event \( x = (l(x), t(x)) \) is a significant real-world thing which happened at location \( l(x) \) and time \( t(x) \). We define the set of events in the same topic domain \( p \) as domain \( X_p \).

Authoritative news outlets are trustworthy sources for event reports. These event reports are not necessarily tweets but can be accesses through public media.

Definition 5. News article: a news article is a collection of event reports generated by authoritative news outlets for a particular event that happened in the past. The set of news articles in the system is expressed as \( A \). The set of news articles in domain \( p \) is expressed as \( A_p \). An article \( a_0 \in A_p \) represents authoritative news reports about event \( x \). Note that one event may be associated with multiple event reports, in which case we merge these event reports into one news article.

Problem definition: given a set of news articles in a specific topic domain as well as a Twitter collection, the problem is to determine user/tweet trustworthiness in this topic domain. More specifically, given a set of events \( X_p \), and a set of news articles \( A_p \) in domain \( p \), as well as a Twitter collection \( C \), the problem of trustworthiness evaluation is to determine the trustworthiness of each tweet \( R(D_i) \) where \( D_i \in D \), and the trustworthiness of each user \( R(U_i) \) where \( U_i \in U \).

To solve this problem, we define the following two tasks:

Task 1: Trust evaluation. Given a set of trustworthy news articles \( A_p \) in domain \( p \), trust evaluation is to calculate the trustworthiness of each tweet \( R(D_i) \) and the trustworthiness of each user \( R(U_i) \) according to the degree of feature similarity between a tweet and the corresponding news article.

Task 2: Trust propagation. Given the ranked tweets, trust propagation is to refine the trustworthiness of users/tweets based on the links defined in the Twitter heterogeneous information network for achieving trust accuracy.

4. Topic-focused similarity-based trust evaluation

In this section, we discuss in detail of our topic-focused similarity-based trust evaluation design. The basic idea is that news articles (see the definition in Section 3) are of high trustworthiness, so we infer trustworthiness from news articles to Twitter users/data in the same topic domain when there is a non-conflictingly contextual similarity including textual, spatial and temporal features. As illustrated in Fig. 1, topic-focused similarity-based trust evaluation has two main components, namely, trustworthiness feature extraction and trustworthiness ranking.

4.1. Trustworthiness feature extraction

The goal of trustworthiness feature extraction is to find the most trustworthy features that can identify a specific event in a topic domain. Although tweets and news articles are quite different in format, they are likely to share some semantic features when describing the same event. We represent these features as domain words and event words. Domain words are the most representative words for an event in a domain. For example, “protest” and “march” can be domain words for “civil unrest” events. Event words are words that can distinguish a particular event from other events in the same domain. For example in a news article describing the “dog protest” event, “YoSoyCan26” and “Zocalo” are event words that rarely appear in other “civil unrest” events. We identify these two types of words through domain weight and event weight defined as follows.

Definition 6. A domain weight \( C(W_i, p) \) quantifies the ability of a word \( W_i \) in representing the topic domain \( p \). Given a news article set \( A_p \) in domain \( p \), and an open-domain document set \( A \), \( C(W_i, p) \) is computed as the product of the normalized term frequency \( f(W_i, A_p) \) of word \( W_i \) in set \( A_p \), and the inverse document frequency of \( W_i \) in set \( A \).

\[
C(W_i, p) = \frac{f(W_i, A_p)}{\max\{f(W, A_p) : W \in A_p\}} \times \log \left( \frac{|A|}{|\{a \in A : W_i \in a\}| + 1} \right) \tag{1}
\]

A domain words set \( W^{(d)}_p \subset W \) is a word subset of words in \( A_p \), containing words with a relatively high domain weight. Initially, all words in \( A_p \) can be viewed as elements in the set of domain words. The first factor in the right side of Eq. (1) is the term frequency of word \( W_i \) [23], and the second factor is the inverse document frequency of \( W_i \) in set \( A \) [24]. Following the popular setting of TF-IDF methods,
the logarithmic is used to “dampen” the effect of inverse document frequency and therefore enhance the impact of term frequency. Based on the domain weight, we remove trivial words with domain weight smaller than a threshold $\eta_d$ calculated by the MAD algorithm [25].

$$\delta_d = \text{median}(\{f(W, A_p) : \forall W \in A_p\})$$  \hspace{1cm} (2)

$$\eta_d = \delta_d + \alpha_d \times \text{median}(\{f(W, A_p) - \delta_d : \forall W \in A_p\})$$  \hspace{1cm} (3)

**Definition 7.** An event word $E(W_i, x)$ quantifies the ability of a word $W_i$ in identifying event $x$. It is computed as the product of the term frequency of word $W_i$ in the news article $a_x$ for event $x$, and the inverse document frequency of $W_i$ in the news article set $A_p$ in domain $p$.

$$E(W_i, x) = \frac{f(W_i, a_x)}{\max(f(W, a_x) : W \in a_x)} \times \log\left(\frac{|A_p|}{|a_x| + 1}\right)$$  \hspace{1cm} (4)

For each event $x$, an event words set $W_{x}^{(d)} \subset W$ is a subset of words in article $a_x$, containing words with a relatively high event weight. Similarly, to remove trivial words from the event words set, we again set a threshold $\delta_e$ computed by the MAD algorithm.

By now, we have obtained domain words and event words from news reports. Next, we use these words as queries to search Twitter data. Only tweets containing at least one domain word or one event word are retrieved and sent to the next module trust ranking.

### 4.2. Trust ranking

In trust ranking module, we evaluate the trustworthiness of tweets. We consider three similarity features.

- **Textual similarity.** We define textual similarity $\phi_{x, D_y}$ between event $x$ and tweet $D_y$ as the product of tweet words’ domain weight sum and event weight sum, as follows:

$$\phi_{x, D_y} = \sum_{W_i \in (D_y, W_{x}^{(d)})} C(W_i, p) \times \sum_{W_i \in (D_y, W_{x}^{(e)})} E(W_i, x)$$  \hspace{1cm} (5)

Only words in the domain word set $W_{x}^{(d)}$ are considered when calculating the domain weight sum, and only words in the event word set $W_{x}^{(e)}$ of event $x$ are considered when computing the event weight sum. There are two reasons behind the formula. The first reason is that, the more domain words and event words one tweet contains, the more likely it will be event-related. Therefore, both the first and the second terms in Eq. (5) are in the form of word weight sum. The second reason is that only tweets containing both domain words and event words are qualified as event-related.

One tweet has many domain words but few event words may discuss other events in the same domain. Likewise, tweet with many event words (e.g., event location names) but few domain words may relate to events in other domains (e.g., something which also happened in the same location). To make a balance between domain words and event words, we multiply the domain weight sum with the event weight sum.

- **Spatial similarity.** Spatial similarity between tweet $D_y$ and event $x$ is decided by two factors: (1) the distance between tweet location $l(D_y)$ and event occurrence location $l(x)$, and (2) the spatial influence scope of tweet $D_y$. The first factor is to relate them to the same location. The second factor is to further enhance the tweet trustworthiness with a high textual-similarity score. Intuitively, within the same distance to the event occurrence location, tweet with a higher textual-similarity score is more likely to be event-related. Therefore, we model a tweet $D_y$’s spatial influence to event $x$ as a Gaussian distribution

$$\varphi_{x, y} = N(x, l(D_y), \sum_x \varphi_{x, y})$$, centered at tweet $D_y$’s location $l(D_y)$, with influence scope $\sum_x \varphi_{x, y}$, where $\phi_{x, y}$ is the textual similarity defined in Eq. (5).

- **Temporal similarity.** After a burst of tweets upon the occurrence of a particular event, the number of event-related tweets usually decreases as a Poisson process [26]. In other words, the possibility of tweet $D_y$ being related with event $x$ decreases as time goes by, i.e., it also decreases following a Poisson process. Therefore, we model temporal similarity between tweet $D_y$ and event $x$ by an exponential distribution.

$$\rho_{x, D_y} = \lambda e^{-|\tau(x) - l(D_y)|}$$ \hspace{1cm} (6)

where $t(x)$ is the occurrence time of event $x$ and $t(D_y)$ is the time-tempo of tweet $D_y$.

By integrating the textual, spatial, and temporal similarity scores, we rank the trustworthiness of tweet $D_y$ for event $x$, $\psi_{x, D_y}$, by the following function:

$$\psi_{x, D_y} = \phi_{x, D_y} \cdot \varphi_{x, y} \cdot \rho_{x, D_y}$$ \hspace{1cm} (7)

In general the trustworthiness of each tweet $D_y$, $R_0(D_y)$, is given by:

$$R_0(D_y) = \{ \psi_{x, D_y}, x \in X_p, D_y \in D \}$$ \hspace{1cm} (8)

For a tweet $D_y$, we choose event $x^*$ that maximizes $\psi_{x, D_y}$ as its most correlated event:

$$x^* = g(D_y) = \arg\max_{x \in X_p} \psi_{x, D_y}$$ \hspace{1cm} (9)

### 5. Trust propagation

#### 5.1. Design principle

Twitter is a social network in which multiple entities exist along with heterogeneous relationships. When evaluating the trustworthiness of an entity in Twitter, the impact from all its neighbor entities in the Twitter heterogeneous information network must be taken into consideration. For example, a user’s trustworthiness can be inferred by looking at the trustworthiness of its posts, and also be influenced by the trustworthiness of his/her friends. The trustworthiness of a tweet can be heavily influenced by the trustworthiness of its author, and can also have relevance to the trustworthiness of other tweets that are semantically or contextually similar to it. Our design principle for trust propagation comprises the following four rules:

- **Rule 1:** If two tweets have a similar (non-conflicting) semantic features, then it is likely they have a similar degree of trustworthiness.

- **Rule 2:** If two tweets have a similar (non-conflicting) conversational context, then they are likely to have a similar degree of trustworthiness.

- **Rule 3:** If a tweet is trustworthy, then the user who posted it is likely to be trustworthy, and other tweets authored by this user are also likely to be trustworthy.

- **Rule 4:** If a user’s friends are trustworthy, then it is likely this user is trustworthy.

#### 5.2. Trust propagation based on semantic or contextual relationship, authorship, or friendship

We follow the four rules discussed in Section 5.1 to execute trust propagation.

- **Trust propagation based on tweet semantic relationship:** based on Rule 1, we do trust propagation from one tweet to another based on their semantic relationship as follows:

$$R_1(D) = \Omega_1 \cdot B \cdot H \cdot B^T \cdot R_0(D)$$ \hspace{1cm} (10)
where $R_0(D)$ is the existing tweet trustworthiness inferred by Eq. (8). $R_1(D)$ is the inferred tweet trustworthiness based on semantic relationships. $B$ is the tweet semantic relationship matrix between all tweet nodes and word nodes, so $B \times B^T$ denotes the word based semantic relationship among all tweet nodes. To reflect the different weights of words on a domain, we define $H$ as:

$$H = \text{diag}(H_1, H_2, \ldots, H_{|W|}), \quad H_i = C(W_i, p)$$

where $C(W_i, p)$ is the domain weight of word $W_i$ on domain $p$ as defined in Eq. (1). $\Omega_1$ is used to normalize the matrix $B \cdot H \cdot B^T$ by column.

- **Trust propagation based on tweet contextual relationship:** based on Rule 2, we do trust propagation from one tweet to another based on their conversational contextual (i.e., replying) relationship as follows:

$$R_2(D) = \Omega_2 \cdot G \cdot R_0(D)$$

where $R_2(D)$ is the inferred tweet trustworthiness based on contextual relationships. $G$ is the tweet replying relationship adjacency matrix where $G_{ij} = 1$ means that tweet $i$ and tweet $j$ have replying conversational relationships, and $G_{ij} = 0$, otherwise. $G$ is column-normalized by $\Omega_2$.

- **Trust propagation based on tweet authorship:** based on Rule 3, we align the credibility of the tweets posted by the same author as follows:

$$R_3(D) = \Omega_3 \cdot E \cdot E^T \cdot R_0(D)$$

where $E$ is the adjacency matrix between all the tweet nodes and the user nodes, and thus the $E \cdot E^T$ represents whether any two tweets share the same author. $R_3(D)$ is the inferred trustworthiness based on authorship relationships. $\Omega_3$ is utilized to normalize the matrix $E \cdot E^T$ by column.

- **Trust propagation based on friendship:** based on Rule 4, we infer the credibility of a tweet based on the author’s credibility in the social network as follows:

$$R_4(D) = \Omega_4 \cdot F \cdot F^T \cdot R_0(D)$$

where $F$ is the adjacency matrix among all the user nodes denoting their friendships. $R_4(D)$ is the inferred trustworthiness based on user friendships. $\Omega_4$ is used to normalize the matrix $F \cdot F^T$ by column.

By combining all the above considerations with appropriate weights, we can get the trust propagation calculated as:

$$R(D) = \lambda_1 \cdot R_1(D) + \lambda_2 \cdot R_2(D) + \lambda_3 \cdot R_3(D) + \lambda_4 \cdot R_4(D)$$

where $\lambda_1$, $\lambda_2$, $\lambda_3$, and $\lambda_4$ with $\lambda_1 + \lambda_2 + \lambda_3 + \lambda_4 = 1$ are weights to allow tradeoffs among these four rules of trust propagation. As a default setting, we set them to $1/4$, which means that they are equally weighted.

5.3. Algorithm description

In this section, we give an algorithmic description of our iterative trust propagation protocol for Twitter (ITPTwitter). ITPTwitter considers context semantics, social network structuring, and user credibility. It is an iterative process by which trust ranking is propagated though the Twitter heterogeneous information network until convergence.

As illustrated by Algorithm 1, the tweet semantic relationship matrix $B$ (related by words), authorship matrix $E$, friendship matrix $F$, replying relationship adjacency matrix $G$ and diagonal word weight matrix $H$ are initialized and given as input. The trustworthiness of entities $R_0^{(1)}(D)$ is initialized to $R_0(D)$. After setting the initial values of $\lambda_1$, $\lambda_2$, $\lambda_3$, and $\lambda_4$ to $1/4$ (for equal contribution) and the iteration number $k = 1$, we propagate trust throughout the social graph iteratively. When the difference between the trustworthiness calculation results in two consecutive iterations falls below a threshold, we stop the iterative process.

**Theorem 1.** The iteration process of ITPTwitter will always converge, that is, the trustworthiness score of any user or tweet in the Twitter heterogeneous information network will converge to a stable value.

**Proof.** We rearrange Eq. (15) and thus have the following equation:

$$R^{(k+1)}(D) = \Gamma \cdot R^{(k)}(D)$$

where $\Gamma$ is the transition matrix between the current trustworthiness score and the next iteration’s trustworthiness score, i.e.,

$$\Gamma = \lambda_1 \cdot BHB^T + \lambda_2 \cdot G + \lambda_3 \cdot EET + (1 - \lambda_1 - \lambda_2 - \lambda_3) \cdot EFE^T$$

According to the “six degrees of separation” theory [27], any user (in a Twitter group) has a path to any other one in a finite number of steps. Hence, $EFE$ is irreducible because its corresponding graph is strongly connected, which ensures that the Markov chain associated with the matrix $\sigma$ is irreducible and aperiodic [28,29]. Finally, the Perron–Frobenius theorem [28] guarantees the existence of a unique stationary distribution vector for the Markov Chain, meaning that $R^{(k)}(D)$ will always converge to a stable value. □

6. Performance evaluation

In this section, we first introduce our performance evaluation methodology and metrics. Then, we describe the experimental settings. Finally we perform a comparative performance analysis of our similarity-based trust evaluation method against two baseline schemes.

6.1. Methodology and metrics

Because of the sheer volume of Twitter data, trust ranking of individual tweets and users is impractical. Instead, we resort to identifying trustworthy tweets while excluding rumors and noise for the Twitter event detection application. Specifically, for Twitter event detection we apply our similarity-based trust evaluation method described in Sections 4 and 5 to collect top tweets with the highest trustworthiness scores in a topic domain (i.e., civil unrest). Then, we
use these high-ranked tweets identified as a training set to a SVM classifier. Next, the trained SVM classifier is applied to new Twitter data to identify emerging events.

We evaluate the effectiveness of our similarity-based trust evaluation method against two baseline schemes:

- Manually ranked tweets: a manually labeled training set is created as input to the same SVM classifier to identify emerging events.
- Tweets generated by [5] based on keyword matching are used as input to the classifier developed in [5] to identify emerging events.

Performance metrics in the experiment include precision, recall, and F-score. Precision quantifies the fraction of detected events (through high-ranked tweets) that match with ground truth events. Recall quantifies the percentage of events that are correctly detected. F-score score is the harmonic mean of precision and recall.

6.2. Experimental settings

6.2.1. Datasets

We use two data sources in the performance evaluation: Twitter and GSR.

- **GSR dataset**: GSR stands for Gold Standard Report (generated by MITRE2), a news dataset specializing in the targeted domain (namely "civil unrest"), in which each GSR event consists of a date, location, and corresponding news reports. A real world event is selected as a GSR event if it is reported by the top 3 news outlets in that country or by influential international media.

- **Twitter dataset**: we randomly selected 10% of raw Twitter data for inclusion in our database. In total, we collected 305 million tweets for this evaluation. To obtain tweet locations, we extracted GPS geo-tags, location mentions, and user profile locations from original Twitter data. Then the extracted entities are mapped to ground-truth locations through a decision tree. There are two matching schemes. One is exact matching, which maps geo-entities into ground-truth locations with exact string match. Another is approximate matching, where a geo-entity is considered a match to a ground truth location if the distance between them is less than a distance threshold. In summary, about 50% of the tweets in the dataset were labelled with country-level locations and 20% with city-level locations.

For both datasets, we collected data across 10 countries in Latin America from July 2012 to May 2013, including: Argentina, Brazil, Chile, Colombia, Ecuador, El Salvador, Mexico, Paraguay, Uruguay, and Venezuela. Table 1 lists more detailed information about Twitter data, news reports sources, and events that happened in each country.

Data from July 2012 to December 2012 are utilized as the training set, and that for January 2013 to May 2013 as the test set. We estimate the trustworthiness of tweets in the training set using our similarity-based trust evaluation method described in Sections 4 and 5 and use the most trustworthy tweets as labels to train the SVM classifier. The trained SVM classifier is then applied to the test set to detect events.

For performance comparison, we also created a manually labeled training set as input to train the SVM classifier. We manually picked tweets related to civil unrest as positive (highly trustworthy) such as "With protests in the Zocalo, # YoSoyCan26 requires Iztapalapa dogs to be free" and left those containing some keywords but irrelevant to civil unrest as negative (lowly trustworthy), such as "Measures should be taken to protect trees against winter damage". To strengthen the quality of training data set, each tweet was assigned to three different annotators. In total, we collected 11,533 tweets in the training set, of which about 46% are "civil unrest related" (positive examples), and 54% are non-related (negative examples).3

There are several parameters that could affect the performance of our method. In the feature extraction module, threshold \( \alpha_c \) in Eq. (3) defines the score boundary \( \eta_c \) between important domain words and trivial ones. Fig. 3 plots weight distribution of top 500 domain words. Tuning points are usually chosen to detect those important "outliers". Notice that there are three obvious tuning points in the curve, near the intersection points with threshold line \( \alpha_c = 0.1, 5, 10 \). A small value of \( \alpha_c \) fails to filter away trivial words. When \( \alpha_c \) is set to be 0.1, the size of domain word set reaches 239. In this case, trivial words such as "yesterday," "adult," and "down" are selected as domain words. On the other hand, a large value of \( \alpha_c \) will remove important words. When \( \alpha_c \) is set up to 10, only 15 words are left as domain words. Therefore, we set \( \alpha_c \) to be 5 (\( \eta_c = 0.09 \)), which returns a medium-size domain word set that contains 52 words.

In the trust ranking module, coefficient \( \lambda \) in Eq. (6) is another tunable parameter. To estimate the value of \( \lambda \), we sample 500 events and fit them to exponential distribution. As a result, we obtain \( \lambda = 0.48 \) with \( R^2 = 0.91 \) on average.

6.3. Trustworthiness of Twitter users

In this section, we validate the assumption that if a Twitter user posts a high percentage of trustworthy tweets, then the user should be more likely to be trustworthy. Although it is almost prohibitive to directly identify whether or not a Twitter user is trustworthy or not, some important Twitter indices are commonly leveraged as surrogates to indicate the Twitter users’ trustworthiness. Specifically, the well-recognized Twitter-author indices are: Account Time Length (the time since the profile was created), Favorite Count, Follower Count, Friends Count, Listed Count (the number of categories interesting the user), and Verified or Not [10].

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2 http://www.mitre.org

Therefore, in our experiments, we evaluate whether there is a positive correlation between the tweets’ trustworthiness weights and their corresponding Twitter-author trustworthiness indices, and whether this positive correlation is statistically significant. In statistics, rank correlation is commonly utilized to measure the relationship between rankings of different ordinal variables, where a “ranking” is the assignment of the labels “first,” “second,” “third,” etc. Specifically, in our experiments, the Spearman correlation [30] is utilized to evaluate the rank correlations between the tweets’ trustworthiness weights and the Twitter-author trustworthiness indices. Moreover, we use p-value to evaluate the statistical significance of the Spearman correlation with the null hypothesis meaning that two sets of data values are Spearman-uncorrelated. A p-value that is equal to or smaller than the significance level (0.03 is used in the paper) means that the null hypothesis is to be rejected, thus supporting the hypothesis that two sets of data values are Spearman-correlated. As can be seen in Table 2, Spearman correlation values between the tweets’ and their authors’ trustworthiness are mostly larger than 0, demonstrating their positive correlation. Moreover, the p-values are mostly less than 0.03, demonstrating strong statistical significance of this positive correlation.

Among all the indices, “Verified or Not” shows a high Spearman correlation, indicating that a verified user seems more likely to post trustworthy tweets, which is reasonable in real-world situations. “Follower Count” also shows that a user with a large number of followers tends to be more trustworthy. Other indices such as “Account Time Length,” “Listed Count,” and “Status Count” endorse strong positive correlation between tweets’ and their authors’ positive correlations, too. Lastly, the index “Favorite count” seems subtle, indicating there is not an apparent correlation between the Twitter users’ trustworthiness and their favorite counts. This also makes sense because an untrustworthy user does not necessarily have a small number of favorites in Twittersphere.

6.4. Comparative performance analysis

6.4.1. Comparison with supervise learning with manually labeled tweets

With the topic domain “civil unrest,” we compare Twitter event detection performance using tweets ranked by our method with that using manually labeled tweets. The performance comparison is shown in Fig. 4. As shown in the figure, our method achieves a higher F-score in 7 out of 10 countries. We make the following two observations:

1. Our method, using automatically ranked tweets, achieves a comparable precision to that of supervised learning using manual labels, and outperforms it in recall and F-score.
2. Our method performs stably across all countries, while the supervised learning using manual labels produces vastly different results across countries. Although the baseline scheme functions better than our method in small countries such as “Paraguay” and “Uruguay,” it falls short in large countries like “Mexico” and “Venezuela,” which occupy more than 32% of total Twitter data and have 46% of total civil unrest events in Latin America.

In summary, our method outperforms the baseline method in both effectiveness and robustness. Namely, our method can yield better results and work more stably across countries. We attribute this to the fact that our method can generate a large amount of high-quality labels for countries with different languages, while it is hard to manually create enough labels with equivalent diversity.

6.4.2. Comparison with supervised learning with Tweets generated through keyword matching

With the topic domain “civil unrest,” we compare Twitter event detection performance using tweets ranked by our method with that based on supervised learning with tweets generated through keyword matching [5]. We show that trustworthy tweets identified by our method are of high quality through both quantitative and qualitative analyses.

Take the small “dog protest” event in Mexico as an example. Table 3 lists the top 3 ranked trustworthy tweets generated by our method using the design concept of similarity-based trustworthiness evaluation and trust propagation against the top 3 ranked trustworthy tweets generated by [5] using keywords most relevant to “civil unrest,” such as “protest” and “march.”

By inspecting Table 3, we make two observations for tweets obtained by [5] through keyword matching:

1. Some tweets are irrelevant to “civil unrest” at all. Take Tweet #3 for example. Its original Spanish text is: “La gente cambia. El amor duele. Los amigos se marchan. Las cosas avances van mal. Pero recuerda que la vida sigue.” Although with one civil unrest keyword “marchan” (becomes “march” after stemming), this tweet is in fact about people’s daily feeling.
2. For those tweets indeed related to “civil unrest,” most of them reflect influential protests that occurred in countries outside Mexico. For example, Tweet #1 is about a protest in Northern Ireland, and Tweet #2 mentions a protest which happened in Venezuelan. Small events such as the “dog protests” are submerged in these big events.

In contrast, trustworthy tweets retrieved by our method are highly related to the “dog protest” event. These tweets can be summarized into two types:

1. Tweets that talk about the protest itself, such as Tweet #1 and Tweet #2. These tweets contain highly ranked “civil unrest” domain words “protesta” (protest) and “marcha” (march), as well as important event words “perrors” (dogs) and “Iztapalapa” (location name).
2. Tweets that are related to the reason of triggering the dog protest event, such as Tweet #3. Here we note that the reason
for triggering the dog protest event is not mentioned in the news report. According to Tweet #3, we find that, citizens protest for the freedom of innocent dogs, which are captured by the Mexico government as suspects for killing 4 people. Besides event words, these tweets also contain middle-ranked domain words such as “Gobierno” (government) and “Mexico,” which are weak indications for “civil unrest” when appearing alone, but get stronger when they co-occur in one tweet.

Table 4 quantitatively compares the trustworthiness and relevance scores of the tweets extracted by the baseline scheme [5] vs. our proposed method. Each tweet was sent to 3 annotators for evaluating whether it is trustworthy or relevant (labeled as True) to the civil unrest topic or not (labeled as False). The tweet is annotated by the labels from the majority of the annotators. The trustworthiness and relevance scores are calculated as the percentage of tweets labeled as True. From Table 4, it is clear that the trustworthiness and relevance of the extracted tweets by the proposed method are much higher than those of the baseline scheme. Our proposed method outperforms the baseline scheme by 15% in trustworthiness, and 6% in relevance. Moreover, the amount of tweets extracted by our method is 14% more than that by the baseline scheme. Our proposed method performs even better in larger countries (e.g., Mexico and Venezuela). We attribute this to our topic-focused similarity-based trust evaluation and trust propagation designs for identifying trustworthy twitters/users, particularly for countries with a large social network.
Table 2
Evaluation of the Trustworthiness of Twitter users. Spearman correlation and p-value with the trustworthiness labels show that our top-ranked trustworthy tweets’ authors are more trustworthy. Here AR = Argentina, BR = Brazil, CH = Chile, CO = Colombia, EC = Ecuador, EL = El Salvador, ME = Mexico, PA = Paraguay, UR = Uruguay, VE = Venezuela, Acco. = Account time length, Favo. = Favorite count, Foll. = Follower count, Frie. = Friend count, List. = Listed count, Stat. = Status count, and Veri. = account verified (1) or Not (0).

<table>
<thead>
<tr>
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</tr>
</thead>
<tbody>
<tr>
<td>AR</td>
<td>0.189</td>
<td>0.057</td>
<td>0.224</td>
<td>0.146</td>
<td>0.257</td>
<td>0.11</td>
<td>0.087</td>
</tr>
<tr>
<td>p-value</td>
<td>0.017</td>
<td>0.012</td>
<td>0.011</td>
<td>0.012</td>
<td>0.014</td>
<td>0.012</td>
<td>0.001</td>
</tr>
<tr>
<td>BR</td>
<td>0.138</td>
<td>0.11</td>
<td>0.166</td>
<td>0.023</td>
<td>0.183</td>
<td>0.148</td>
<td>0.076</td>
</tr>
<tr>
<td>p-value</td>
<td>0.012</td>
<td>0.011</td>
<td>0.012</td>
<td>0.012</td>
<td>0.014</td>
<td>0.012</td>
<td>0.003</td>
</tr>
<tr>
<td>CH</td>
<td>-0.002</td>
<td>0.055</td>
<td>0.125</td>
<td>0.046</td>
<td>0.143</td>
<td>0.08</td>
<td>-0.067</td>
</tr>
<tr>
<td>p-value</td>
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<td>0.009</td>
<td>0.01</td>
<td>0.024</td>
<td>0.005</td>
<td>0.017</td>
<td>0.016</td>
</tr>
<tr>
<td>CO</td>
<td>-0.022</td>
<td>0.109</td>
<td>0.22</td>
<td>-0.038</td>
<td>0.125</td>
<td>0.034</td>
<td>0.047</td>
</tr>
<tr>
<td>p-value</td>
<td>0.015</td>
<td>0.022</td>
<td>0.027</td>
<td>0.015</td>
<td>0.004</td>
<td>0.035</td>
<td>0.023</td>
</tr>
<tr>
<td>EC</td>
<td>0.131</td>
<td>0.141</td>
<td>0.474</td>
<td>0.249</td>
<td>0.479</td>
<td>0.309</td>
<td>0.531</td>
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<tr>
<td>p-value</td>
<td>0.052</td>
<td>0.009</td>
<td>0.011</td>
<td>0.009</td>
<td>0.007</td>
<td>0.032</td>
<td>0.004</td>
</tr>
<tr>
<td>EL</td>
<td>-0.11</td>
<td>0.363</td>
<td>0.031</td>
<td>0.002</td>
<td>0.395</td>
<td>0.254</td>
<td>N/A</td>
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<td>p-value</td>
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<tr>
<td>ME</td>
<td>0.122</td>
<td>-0.092</td>
<td>0.188</td>
<td>-0.018</td>
<td>0.193</td>
<td>0.117</td>
<td>0.189</td>
</tr>
<tr>
<td>p-value</td>
<td>0.003</td>
<td>0.004</td>
<td>0.004</td>
<td>0.013</td>
<td>0.002</td>
<td>0.003</td>
<td>0.002</td>
</tr>
<tr>
<td>PA</td>
<td>0.194</td>
<td>0.202</td>
<td>0.39</td>
<td>0.173</td>
<td>0.346</td>
<td>0.345</td>
<td>0.385</td>
</tr>
<tr>
<td>p-value</td>
<td>0.027</td>
<td>0.014</td>
<td>0.019</td>
<td>0.043</td>
<td>0.019</td>
<td>0.013</td>
<td>0.023</td>
</tr>
<tr>
<td>UR</td>
<td>0.245</td>
<td>0.053</td>
<td>0.333</td>
<td>-0.003</td>
<td>0.387</td>
<td>0.282</td>
<td>0.38</td>
</tr>
<tr>
<td>p-value</td>
<td>0.009</td>
<td>0.021</td>
<td>0.005</td>
<td>0.036</td>
<td>0.002</td>
<td>0.001</td>
<td>0.011</td>
</tr>
<tr>
<td>VE</td>
<td>0.171</td>
<td>-0.111</td>
<td>0.259</td>
<td>0.079</td>
<td>0.244</td>
<td>-0.051</td>
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<tr>
<td>p-value</td>
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<td>0.005</td>
<td>0.001</td>
<td>0.011</td>
<td>0.001</td>
<td>0.002</td>
<td>0.002</td>
</tr>
</tbody>
</table>

Table 3
Comparing tweets collected for the dog protect event in Mexico. Domain words are denoted by bold style and event words are marked with underline. The tweets, originally in Spanish, have been translated into English using Google Translate.

| 1. Northern Ireland live another march day: demonstrators protest since December by a decree restricting dog ownership http://t.co/O2K9hMiq |
| Tweets by [5] |
| 2. #EnImágenes Students protest in several states against the judgment of the Supreme Court http://t.co/cfj5X5sA |

| 1. With protests in the Zócalo, #YoSoyCan26 requires government to free dogs of Iztapalapa http://t.co/3PsQ90po AMLO |
| Tweets by our method |
| 2. #YoSoyCan26 march in solidarity with, Socket for victims’ families in Cerro de la Estrella and demand liberty for dogs. |
| 3. RT @politicomex: To people of Mexico, dogs are murderers is incredulous: Government of the capital is asked to clarify the truth... http://t.co/m5UbmJXT |

Table 4
Quantitative performance comparison of our proposed method with the baseline scheme [5] in the Trustworthiness and Relevance scores of extracted Tweets (Trust. = Trustworthiness Score, Relev. = Relevance score).

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Trust. (%)</td>
<td>Relev. (%)</td>
</tr>
<tr>
<td>Argentina</td>
<td>67</td>
<td>71</td>
</tr>
<tr>
<td>Brazil</td>
<td>62</td>
<td>76</td>
</tr>
<tr>
<td>Chile</td>
<td>66</td>
<td>70</td>
</tr>
<tr>
<td>Colombia</td>
<td>70</td>
<td>82</td>
</tr>
<tr>
<td>Ecuador</td>
<td>65</td>
<td>68</td>
</tr>
<tr>
<td>El Salvador</td>
<td>56</td>
<td>68</td>
</tr>
<tr>
<td>Mexico</td>
<td>74</td>
<td>85</td>
</tr>
<tr>
<td>Paraguay</td>
<td>83</td>
<td>70</td>
</tr>
<tr>
<td>Uruguay</td>
<td>71</td>
<td>68</td>
</tr>
<tr>
<td>Venezuela</td>
<td>75</td>
<td>78</td>
</tr>
<tr>
<td>Total</td>
<td>71</td>
<td>78</td>
</tr>
</tbody>
</table>

7. Conclusion

In this paper, we proposed a new design notion of topic-focused similarity-based trust evaluation and trust propagation to rate trustworthiness of tweets and users in Twitter. Compared to existing methods, our approach has three advantages: (1) enabling context-based trustworthiness estimation to focus on credibility in a specific topic domain; (2) utilizing credible news reports to infer trustworthiness of tweets exhibiting contextual similarity in textual, spatial and temporal features; and (3) combining semantic and contextual information with social networking information for trustworthiness propagation. Experiments on Twitter event detection...
demonstrated that our method can effectively extract trustworthy tweets while excluding rumors and noise. In addition, a comparative performance analysis demonstrated that our method outperforms existing supervised learning schemes using tweets manually labeled or tweets generated based on keyword matching as the training set.

This paper assumes persistent attack behavior, i.e., a malicious user attacks without disguise whenever it has a chance. In the future, we plan to consider more sophisticated attack behaviors such as random, opportunistic, and insidious attack behaviors [31–34] to further test the robustness of our topic-focused similarity-based trust evaluation scheme.

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References